

# higher education & training

Department:  
Higher Education and Training  
**REPUBLIC OF SOUTH AFRICA**

## **MARKING GUIDELINE**

**NATIONAL CERTIFICATE (VOCATIONAL)**

**APRIL EXAMINATION**

**POWER MACHINES N5**

**14 APRIL 2015**

**This marking guideline consists of 9 pages.**

## QUESTION 1

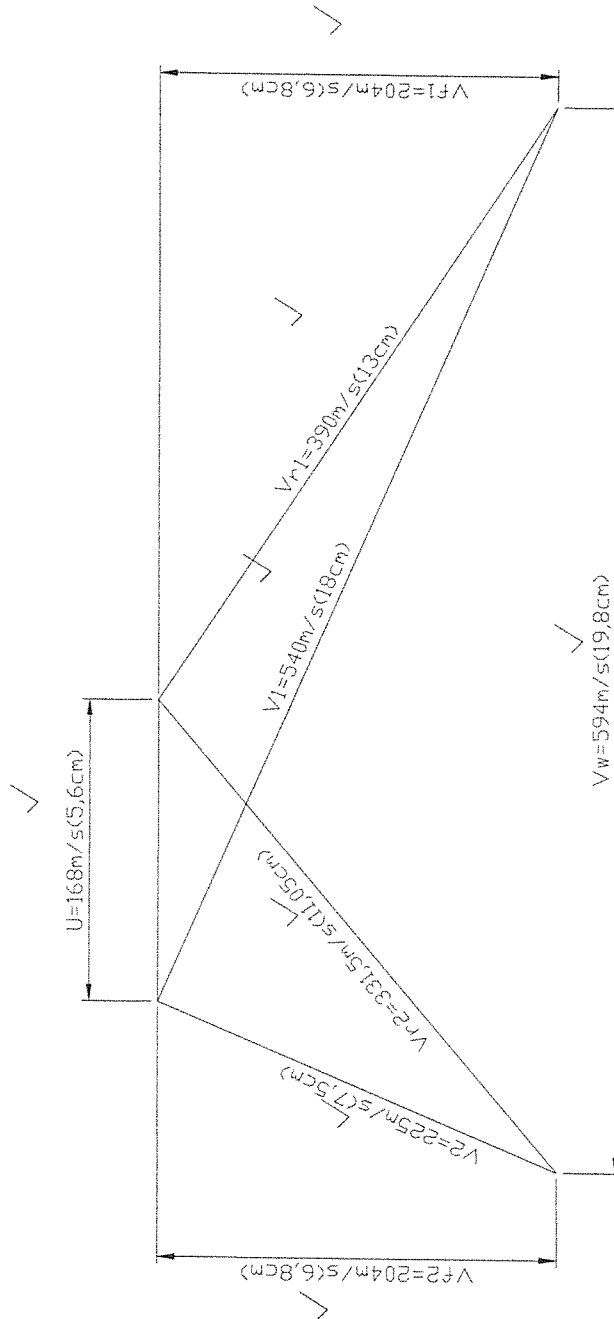
- 1.1 1.1.1  $HCV = \frac{(M_w + W_e)C_p \times \Delta t}{M_f} \quad \checkmark$   
 $= \frac{(2,464 + 0,327)4,2 \times (20,69 - 18,5)}{7 \times 10^{-4}} \quad \checkmark$   
 $= 36673,74 \text{ kJ / kg} \quad \checkmark$   
 $= \boxed{36,67 \text{ MJ / kg}} \quad \checkmark \quad (4)$
- 1.1.2  $LCV = HCV \times (100\% - 13,7\%) \quad \checkmark$   
 $= 36,67 \times 86,3\% \quad \checkmark$   
 $= 31,646 \text{ MJ / kg}$   
 $= \boxed{31,65 \text{ MJ / kg}} \quad \checkmark \quad (3)$
- 1.1.3  $LCV = HCV - \left( hfg \times 9 \times \frac{H_2}{100} \right) \quad \checkmark$   
 $H_2 = \frac{HCV - LCV}{hfg \times 9} \times \frac{100}{1} \quad \checkmark$   
 $= \frac{36,67 - 31,65}{2,453 \times 9} \times \frac{100}{1} \quad \checkmark$   
 $= 0,22738 \times \frac{100}{1}$   
 $= \boxed{22,74\%} \quad \checkmark \quad (3)$
- 1.2 1.2.1  $Mass\ of\ air = \frac{100}{23} \left[ \frac{8}{3}C + 8H_2 + S - O_2 \right] \quad \checkmark$   
 $= \frac{100}{23} \left[ \left( \frac{8}{3} \times 0,86 \right) + (8 \times 0,07) - 0,07 \right] \quad \checkmark$   
 $= 12,1 \text{ kg / kg fuel} \quad \checkmark$   
 $\therefore Total\ mass = 12,1 \times 12$   
 $= \boxed{145,2 \text{ kg}} \quad \checkmark \quad (4)$
- 1.2.2  $HCV = (HV_c \times C) + HV_{H_2} H_2 \frac{O_2}{8} + (HV_s \times S) \quad \checkmark$   
 $= (35 \times 0,86) + 144 \times 0,07 \frac{0,07}{8} \quad \checkmark$   
 $= \boxed{38,92 \text{ MJ}} \quad \checkmark \quad (3)$

$$\begin{aligned} 1.2.3 \quad \text{LCV} &= \text{HCV} \quad (\text{hfg} \times 9 \times \text{H}_2) && \checkmark \\ &= 38,92 \quad (2,424 \times 9 \times 0,07) && \checkmark \\ &= \boxed{37,393 \text{ MJ/kg}} && \checkmark \end{aligned}$$

(3)  
[20]

**QUESTION 2**

2.1	$U$	=	$\pi \times D \times N$	✓	$V_{r_2}$	=	$V_{r_1} \times K$	✓
		=	$\frac{\pi \times 0,46 \times 6976}{60}$	✓		=	$390 \times 0,85$	✓
		=	$168 \text{ m/s}$	✓		=	$331,5 \text{ m/s}$	✓



(14)

$$\begin{aligned}
 2.2 \quad 2.2.1 \quad P &= MUV_w \quad \checkmark \\
 &= 1 \times 168 \times 594 \quad \checkmark \\
 &= 99792 \text{ W} \\
 &= \boxed{99,792 \text{ kW}} \quad \checkmark
 \end{aligned}$$

(3)

$$\begin{aligned}
 2.2.2 \quad KE &= \frac{1}{2} MV^2 \quad \checkmark \\
 &= 0,5 \times 1 \times 225^2 \quad \checkmark \\
 &= 25312,5 \text{ W/kg} \\
 &= \boxed{25,313 \text{ kW/kg}} \quad \checkmark
 \end{aligned}$$

(3)  
[20]

## QUESTION 3

3.1

Given:

$V_{\text{air}} = 18,5 \text{ m}^3/\text{min}$

$P_1 = 110 \text{ kPa}$

$N = 400 \text{ r/min}$

$n = 1,35$

Double-Acting

$T_1 = 295 \text{ K}$

$P_2 = 820 \text{ kPa}$

$V_c = 0,07S_v$

$$\begin{aligned}
 3.1.1 \quad V_1 &= V_3 + S_v \quad \checkmark \\
 &= 0,07S_v + S_v
 \end{aligned}$$

$$V_1 = 1,07S_v \quad \langle 1 \rangle \quad \checkmark$$

$$V_4 = V_3 \frac{P_2}{P_1}^{\frac{1}{n}} \quad \checkmark$$

$$= 0,07S_v \frac{820}{110}^{\frac{1}{1,35}}$$

$$= 0,31S_v \quad \checkmark \langle 2 \rangle$$

$$\frac{V_1}{1,07S_v} = \frac{V_4}{0,31S_v} = 18,5 \text{ m}^3/\text{min} \quad \checkmark$$

$$0,76S_v = 18,5 \quad \checkmark$$

$$S_v = 24,3421 \text{ m}^3/\text{min} \quad \checkmark$$

$$\therefore S_v = 24,3421 \text{ m}^3/\text{min} \quad \checkmark$$

$$\therefore S_v = \frac{24,3421}{400 \times 2} \quad \checkmark$$

$$= \boxed{0,030428 \text{ m}^3} \quad \checkmark$$

(10)

$$\begin{aligned}
 3.1.2 \quad \frac{T_2}{T_1} &= \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} && \checkmark \\
 T_2 &= T_1 \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \\
 &= 295 \left( \frac{820}{110} \right)^{\frac{1,35-1}{1,35}} && \checkmark \\
 &= \boxed{496,6 \text{ K}} && \checkmark
 \end{aligned}
 \tag{3}$$

$$\begin{aligned}
 3.1.3 \quad P &= P_1 V_1 \frac{n}{n-1} \left[ \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} - 1 \right] && \checkmark \\
 &= 110 \times \frac{18,5}{60} \times \left( \frac{1,35}{1,35-1} \right) \times \left[ \left( \frac{820}{110} \right)^{\frac{1,35-1}{1,35}} - 1 \right] && \checkmark \\
 &= \boxed{89,4 \text{ kW}} && \checkmark
 \end{aligned}
 \tag{3}$$

3.2 Dalton's law of partial pressure states that the pressure of a mixture of gases equals the sum of the partial pressures of each individual gas at the same temperature, in the container.  $\checkmark$  (2)

3.3 Axial – flow turbines  $\checkmark$

Radial – flow turbines  $\checkmark$

(2)  
[20]

## QUESTION 4

Given:

$$\begin{array}{llll}
 P_2 & = & 655 \text{ kPa} & PV^n = C & V_1 & = & 0,114 \text{ m}^3 \\
 P_1 & = & 110 \text{ kPa} & T_1 & = & 373 \text{ K} & V_2 & = & \frac{1}{4} \text{ of } V_1 \\
 C_v & = & 0,754 \text{ kJ/kg.K} & & & & C_p & = & 1,05 \text{ kJ/kg.K}
 \end{array}$$

$$\begin{array}{llll}
 4.1 & R & = & C_p - C_v & \checkmark \\
 & & = & 1,05 - 0,754 & \checkmark \\
 & & = & 0,296 \text{ kJ/kg.K} & \checkmark
 \end{array}$$

$$\begin{array}{llll}
 P_1 V_1 & = & M R T_1 & \\
 M & = & \frac{P_1 V_1}{R T_1} & \checkmark \\
 & = & \frac{110 \times 0,114}{0,296 \times 373} & \checkmark \\
 & = & \boxed{0,1136 \text{ kg}} & \checkmark
 \end{array}$$

(6)

$$\begin{array}{llll}
 4.2 & V_2 & = & \frac{1}{4} \text{ of } V_1 & \checkmark \\
 & & = & 0,25 \times 0,114 & \\
 & & = & 0,0285 \text{ m}^3 & \checkmark
 \end{array}$$

$$\begin{array}{llll}
 P_1 V_1^n & = & P_2 V_2^n & \\
 \left(\frac{V_1}{V_2}\right)^n & = & \frac{P_2}{P_1} & \checkmark \\
 n \ln \frac{V_1}{V_2} & = & \ln \frac{P_2}{P_1} & \checkmark \\
 \therefore n & = & \frac{\ln \left(\frac{P_2}{P_1}\right)}{\ln \left(\frac{V_1}{V_2}\right)} & \checkmark \\
 & = & \frac{\ln \left(\frac{655}{110}\right)}{\ln \left(\frac{0,114}{0,0285}\right)} & \checkmark \\
 & = & \frac{1,78415}{1,38629} & \\
 & = & \boxed{1,287} & \checkmark
 \end{array}$$

(7)

$$\begin{aligned}
 4.3 \quad \frac{P_1 V_1}{T_1} &= \frac{P_2 V_2}{T_2} && \checkmark \\
 T_2 &= \frac{P_2 V_2 T_1}{P_1 V_1} && \\
 &= \frac{655 \times 0,0285 \times 373}{110 \times 0,114} && \checkmark \\
 &= \boxed{555,26 \text{ K}} && \checkmark
 \end{aligned}$$

or

$$\begin{aligned}
 T_2 &= T_1 \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} && \checkmark \\
 &= 373 \left( \frac{655}{110} \right)^{\frac{1,287-1}{1,287}} && \checkmark \\
 &= \boxed{555,26 \text{ K}} && \checkmark
 \end{aligned}$$

(3)

$$\begin{aligned}
 4.4 \quad S_1 - S_2 &= m \left\{ \left( C_v \ln \frac{T_2}{T_1} \right) + \left( R \ln \frac{V_2}{V_1} \right) \right\} && \checkmark \\
 &= 0,1136 \left\{ \left( 0,754 \ln \frac{555,26}{373} \right) + \left( 0,296 \ln \frac{0,0285}{0,114} \right) \right\} && \checkmark \\
 &= 0,1136 \{ 0,29998 + (-0,41034) \} && \\
 &= \boxed{-0,01254 \text{ kJ / K}} && \checkmark
 \end{aligned}$$

(4)  
[20]

## QUESTION 5

5.1

Given:

$$M = 3,5 \text{ kg}$$

$$t_{su} = 300 \text{ }^\circ\text{C}$$

$$P_2 = 280 \text{ kPa}$$

$$P_1 = 2000 \text{ kPa}$$

$$x = 0,9$$

$$C_p = 2,1 \text{ kJ/kg}\cdot\text{K}$$

$$\begin{aligned} U_1 &= h - P_1 V_1 \quad (@ 2000 \text{ kPa and } 300^\circ\text{C}) \quad \checkmark \\ &= \{hg + C_p(t_{su} - t_s)\} - \left\{ P_1 \times \left[ \frac{0,231(h_{sup} - 1941)}{P_1} \right] \right\} \quad \checkmark \\ &= \{2797 + 2,1(300 - 212,4)\} - \left\{ 2000 \times \left[ \frac{0,231(3025 - 1941)}{2000} \right] \right\} \quad \checkmark \\ &= 2980,96 - 250,404 \\ &= 2730,556 \text{ kJ/kg} \quad \checkmark \end{aligned}$$

$$\begin{aligned} U_2 &= h - P_2 V_2 \quad (@ 280 \text{ kPa and } x = 0,9) \quad \checkmark \\ &= \{hf + xhfg\} - \{P_2 \times xVg_2\} \quad \checkmark \\ &= \{551 + (0,9 \times 2170)\} - \{280(0,9 \times 0,6460)\} \quad \checkmark \\ &= 2504 - 162,792 \\ &= 2341,208 \text{ kJ/kg} \quad \checkmark \end{aligned}$$

$$\begin{aligned} U_2 - U_1 &= 2341,208 - 2730,556 \quad \checkmark \\ &= -389,348 \text{ kJ/kg} \quad \checkmark \end{aligned}$$

$$\begin{aligned} \therefore \Delta U &= 3,5(U_2 - U_1) \quad \checkmark \\ &= 3,5 \times (-389,348) \quad \checkmark \\ &= \boxed{-1362,718 \text{ kJ}} \quad \checkmark \end{aligned}$$

(17)

5.2 Solid – eg Ice  
Liquid – eg Water  
Gas – eg Steam

(3)  
[20]

TOTAL: 100